

4-3: Solving Multi-Step Inequalities

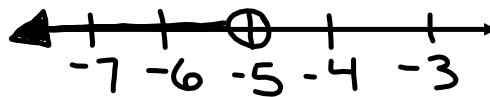
Solve Multi-Step Inequalities Multi-step inequalities can be solved by undoing the operations in the same way you would solve a multi-step equation.

1. Solve $-11y - 13 > 42$. Graph the solution on a number line.

divided by a negative # \rightarrow

$$\begin{array}{r} -11y - 13 > 42 \\ -11y > 55 \\ \hline -11y > 55 \\ \hline y < -5 \end{array}$$

original inequality
Addition Prop. (+13 each side)
Division Prop. ($\div -11$ each side)
Simplify



TRY SOME: Solve each inequality. Check your solution.

2. $23 \geq 10 - 2w$

$$\begin{array}{r} 23 \geq 10 - 2w \\ -10 \quad -10 \downarrow \\ \hline 13 \geq -2w \\ \hline -2 \quad -2 \\ \hline -6.5 \leq w \\ w \geq -6.5 \end{array}$$

3. $43 > -4y + 1$

$$\begin{array}{r} 43 > -4y + 1 \\ -11 \quad -11 \downarrow \\ \hline 32 > -4y \\ \hline -4 \quad -4 \\ \hline -8 < y \end{array}$$

$\rightarrow y > -8$

Now, how about something a bit more challenging:

4. $6(5z - 3) \leq 36z$

$$\begin{array}{r} 30z - 18 \leq 36z \\ -30z \quad -30z \\ \hline -18 \leq 6z \\ \hline -3 \leq z \\ z \geq -3 \end{array}$$

5. $2(h + 6) > -3(8 - h)$

$$\begin{array}{r} 2h + 12 > -24 + 3h \\ -2h \quad -2h \\ \hline 12 > -24 + h \\ +24 \quad +24 \\ \hline 36 > h \\ h < 36 \end{array}$$

Solve each inequality, check your solution. Does anything "weird" happen?

$$6. \quad 9t - 5(t - 5) \leq 4(t - 3)$$

$$9t - 5t + 25 \leq 4t - 12$$

$$\begin{array}{r} 4t + 25 \leq 4t - 12 \\ -4t \quad \downarrow \quad -4t \quad \downarrow \\ \hline 25 \leq -12 \end{array}$$

FALSE → NO SOLUTION!

When your variables cancel out, leaving a FALSE inequality, there is NO SOLUTION. \emptyset

$$7. \quad 3(4m + 6) \leq 42 + 6(2m - 4)$$

$$12m + 18 \leq 42 + 12m - 24$$

$$\begin{array}{r} 12m + 18 \leq 12m + 18 \\ -12m \quad \downarrow \quad -12m \quad \downarrow \\ \hline \text{True } 18 \leq 18 \end{array}$$

infinite solutions

When your variables cancel out, leaving a TRUE inequality, ALL VALUES are solutions. This is called an IDENTITY.

Define a variable, write an inequality, and solve each problem. Then interpret your solution.

8. Keith's dog weighs 90 pounds. A healthy weight for his dog would be less than 75 pounds. If Keith's dog can lose an average of 1.25 pounds per week on a certain diet, after how long will the dog reach healthy weight?

$w = \text{weeks}$

$$\begin{array}{r} 90 - 1.25w < 75 \\ -90 \quad \downarrow \quad -90 \\ \hline -1.25w < -15 \\ = -1.25 \quad = -1.25 \end{array}$$

$w > 12$
After 12 weeks

9. A high school drama club is performing a musical to benefit a local charity. Tickets are \$5 each. They also received donations of \$565. They want to raise at least \$1500.

$t = \text{tickets}$

- a. Write an inequality that describes this situation. Then solve the inequality.

$$5t + 565 \geq 1500$$

$$\begin{array}{r} \downarrow -565 \quad | \quad -565 \\ \hline 5t \geq 935 \\ \hline t \geq 187 \end{array}$$

- b. Graph the solution.



closed circle because \geq means we include 187.

$t \geq 187$
At least 187 tickets must be sold.